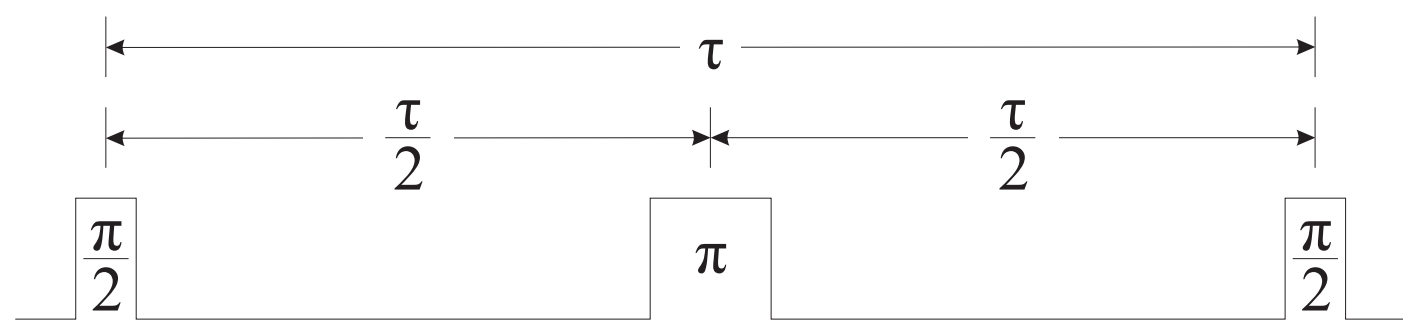


Dynamical Decoupling of a $^{43}\text{Ca}^+$ Memory Qubit

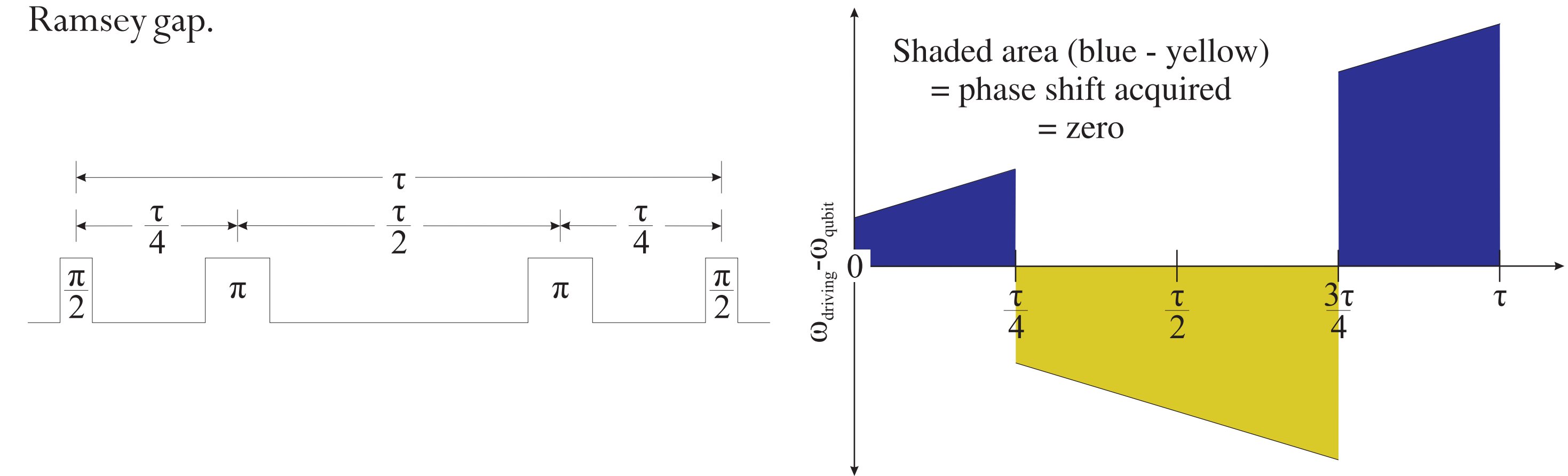
Ion Trap Quantum Computing Group - Department of Physics - University of Oxford

Generalised Spin-Echo to Protect Against Changing Magnetic Field

The Hahn spin-echo is a well-known method to improve the coherence of a Ramsey experiment, if the frequency of the atom's free precession is slightly different to the driving radiation. A π -pulse in the middle of the gap can "unwind" the excess phase acquired from this offset, and restore the fringe contrast.



Any variation in the frequency error, such as a drifting magnetic field, will cause an uncorrected error. However, we see by inspection that two π -pulses can precisely cancel out the error if the frequency is varying linearly with time. They must be placed at times $t = \tau/4$ and $t = 3\tau/4$, where τ is the total Ramsey gap.



To generalise further, suppose the detuning $\delta(t)$ is an $(n-1)$ th order polynomial with time: $\delta(t) = a_0 + a_1 t + a_2 t^2 + \dots + a_{n-1} t^{n-1}$. Perfect, instantaneous π -pulses occur at times $\alpha_1 \tau, \alpha_2 \tau, \dots, \alpha_n \tau$. The spurious accumulated phase ϕ_{err} is given by integrating the detuning with respect to time, so demanding that ϕ_{err} vanishes requires us to solve:

$$0 = \phi_{err} = \int_0^{\alpha_1} \delta(t) dt - \int_{\alpha_1}^{\alpha_2} \delta(t) dt + \dots + (-1)^n \int_{\alpha_n}^1 \delta(t) dt$$

$$= \left[a_0 t + \frac{a_1}{2} t^2 + \dots + \frac{a_{n-1}}{n} t^n \right]_0^{\alpha_1} - \left[a_0 t + \frac{a_1}{2} t^2 + \dots + \frac{a_{n-1}}{n} t^n \right]_{\alpha_1}^{\alpha_2} + \dots$$

$$+ (-1)^n \left[a_0 t + \frac{a_1}{2} t^2 + \dots + \frac{a_{n-1}}{n} t^n \right]_{\alpha_n}^1$$

$$= \sum_{j=0}^{n-1} \frac{a_j}{j+1} \left(2 \sum_{i=1}^n (-1)^i \alpha_i^j + (-1)^n \right)$$

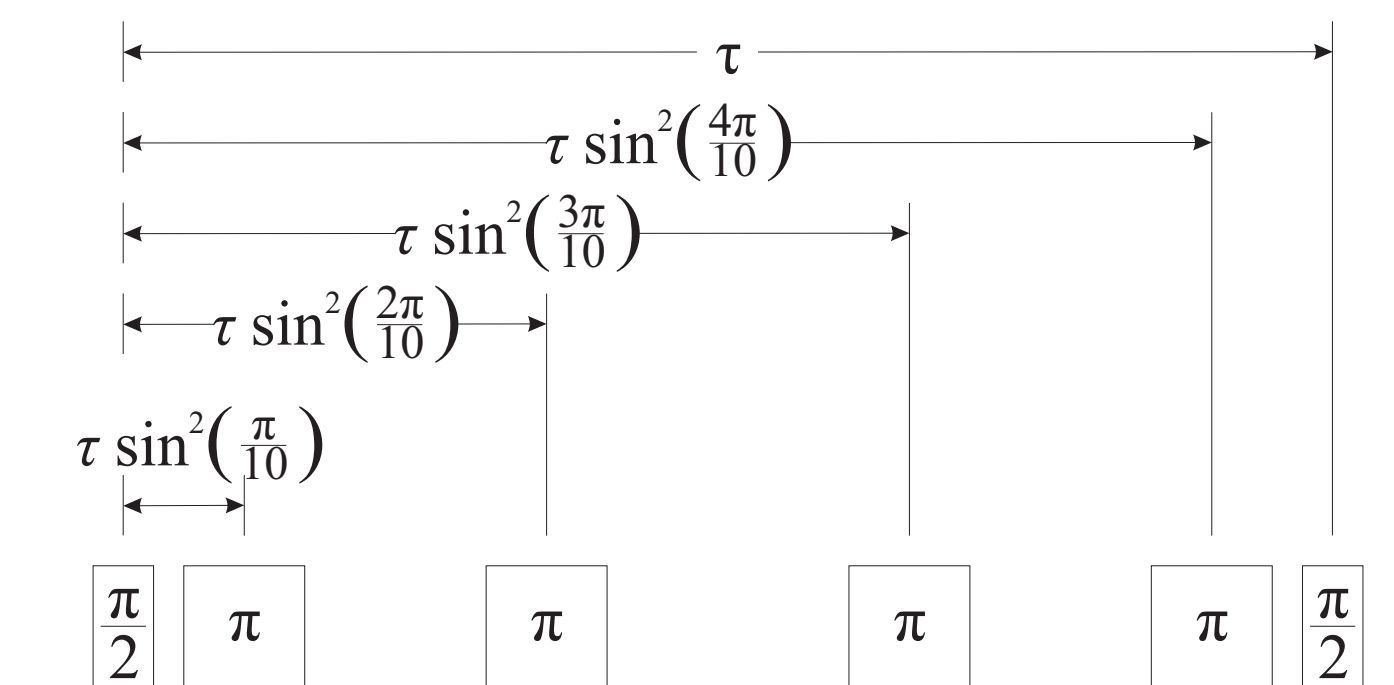
This equation must be independently true for each polynomial coefficient a_j , because they can take any (real) value. So we obtain a set of simultaneous equations:

$$(-1)^n + 2 \sum_{i=1}^n (-1)^i \alpha_i^j = 0 \quad \forall j = 1, 2, \dots, n.$$

These simultaneous equations are solved when the pulse times α_i take the values:

$$\alpha_i = \sin^2 \left(\frac{\pi i}{2n+1} \right)$$

This pulse sequence is illustrated below for $n=4$.

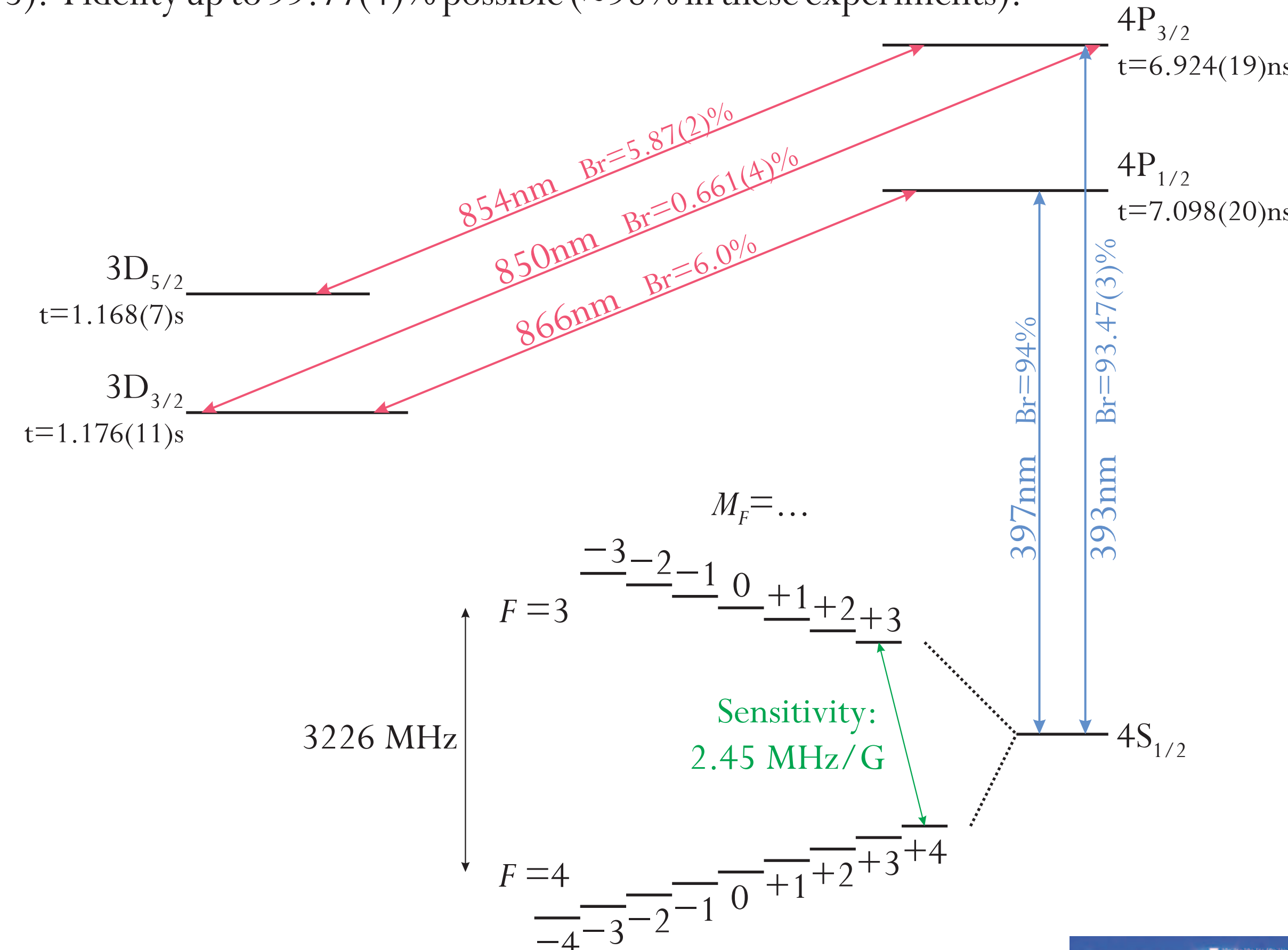


An n pulse sequence precisely cancels out the spurious accumulated phase when the detuning is an $(n-1)$ th order polynomial in time.

This sequence is called Uhrig Dynamical Decoupling (UDD). Previously discovered in a solid-state context, by considering a spin-echo sequence as a frequency domain filter. See: "Exact results on dynamical decoupling by π pulses in quantum information processes", Götz S Uhrig, New Journal of Physics **10** (2008) 083024. Biercuk *et al.* have implemented UDD on an ensemble of ions in a Penning trap: "Experimental Uhrig dynamical decoupling using trapped ions", Michael J Biercuk *et al.*, Physical Review A **79** (2009) 062324.

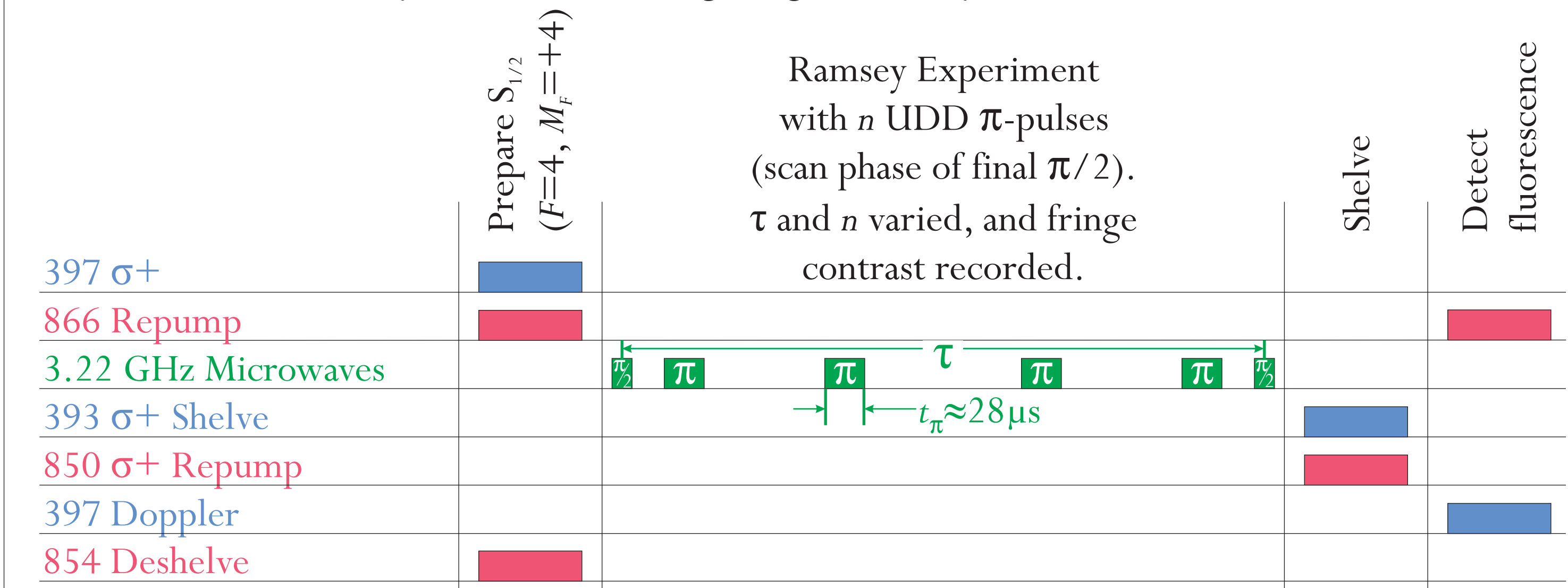
$^{43}\text{Ca}^+$ Hyperfine Qubit

- Qubit stored in $S_{1/2}$ hyperfine-split level: $(F=3, M_F=+3)$ and $(F=4, M_F=+4)$ states.
- Sensitive to magnetic field: 2.45 MHz/gauss. 3.226 GHz at zero field. Work at 2.4 GHz. Rabi frequency up to 18 kHz ($t_\pi \approx 28 \mu\text{s}$).
- Doppler cooling, and observation of fluorescence, at 397 nm. Repump at 866 nm.
- Readout: use 393 nm to shelve ion in $D_{3/2}$, with 850 nm to repump from $D_{3/2}$. Frequency selective - shelve only from $S_{1/2}(F=4)$. Then apply 397 nm + 866 nm and observe fluorescence only if ion was in $S_{1/2}(F=3)$. Fidelity up to 99.77(4)% possible ($\approx 98\%$ in these experiments).



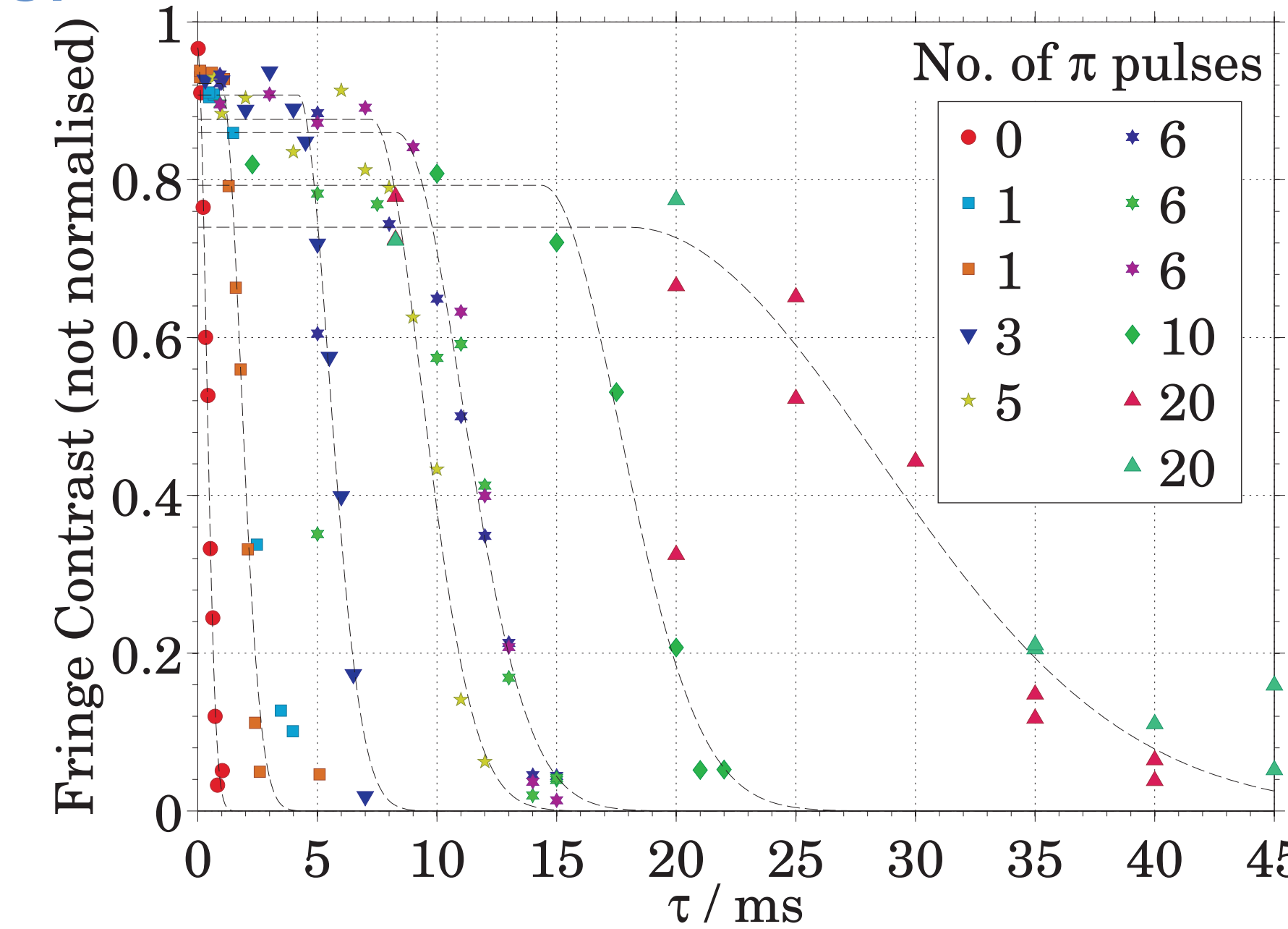
Experimental Results

We have implemented Dynamical Decoupling using the $^{43}\text{Ca}^+$ hyperfine qubit.

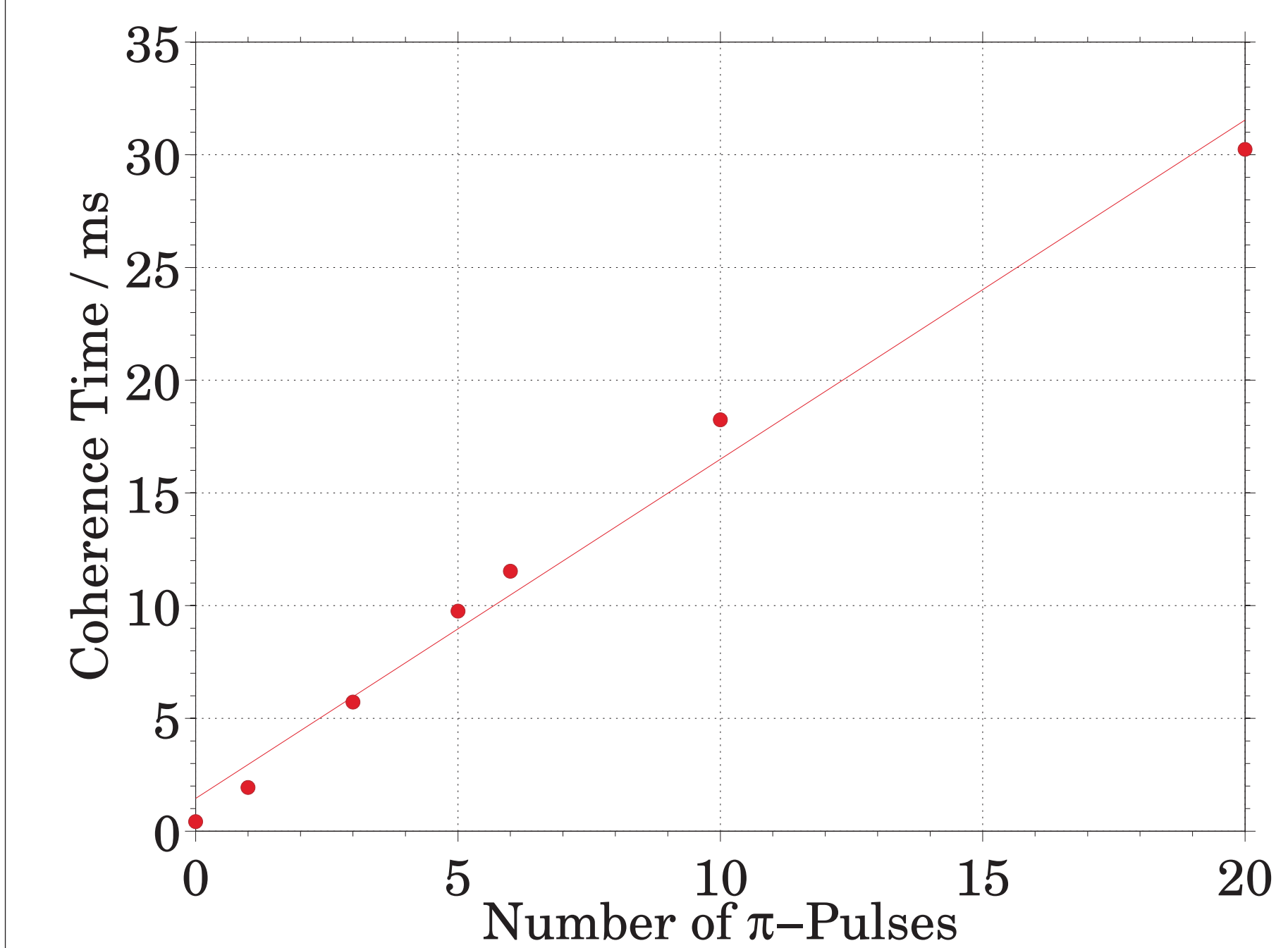


Coherence time increased from 0.45 ms (no π -pulses) to ≈ 28 ms with 20 π -pulses.

Plot the Ramsey fringe contrast against the total time τ . The different symbols denote the number of π -pulses used for that sequence; different colours for the same symbol indicate data from different days.



Black dashed lines are fits to guide the eye. Consisting of a flat line followed by a half-Gaussian, they do not represent any physical model.



For each of the above fits, the time at which the curve reached half its initial value is a measure of the coherence time. These times are plotted against the number of pulses, and fitted with a straight line.

UDD could also be performed using the magnetic-field insensitive $M_F=0$ "clock" states. Previously, we used a single spin-echo pulse on such a qubit and observed negligible ($\approx 1\%$) decoherence in 1 s. Dynamical decoupling could extend this even further. See: "A long-lived memory qubit on a low-decoherence quantum bus", David M Lucas *et al.*, arXiv:0710.4421 [quant-ph].